## Flow Documentation

The measurements were made in the Virginia Polytechnic Institute and State University Stability Wind Tunnel. This tunnel is a continuous, closed return, subsonic wind tunnel with a 7 m long and 1.8 m square test section. The regulated fan d.c. power source, a 9:1 area contraction, and seven wire-mesh screens provide low free-stream turbulence levels - of the order of $0.03 \%$.

The $6: 1$ prolate spheroid used for these measurements is 1.37 m long and is constructed of a machined fiberglass skin bonded to an aluminum frame. A circumferential trip, consisting of posts 1.2 mm in diameter, 0.7 mm high and spaced 2.5 mm apart, was placed around the model at $x / L=0.2$. This fixed the location of transition. Windows of size $30 \times 150 \times 0.75 \mathrm{~mm}$ were placed in the skin for optical (LDV) access to the flow ${ }^{1,5,6}$. The windows were molded to the curvature of the model and mounted flush with the model surface in order to minimize flow disturbances. Wax was used to fill any small gaps in the model surface. The model was supported with a rear-mounted, 0.75 m long sting aligned along the model axis and connected to a vertical post extended through the wind tunnel floor. All measurements were conducted at a constant Reynolds number, $R e_{L}=4.20 \times 10^{6},\left(50.73 \mathrm{~m} / \mathrm{s}<U_{\infty}<55.25 \mathrm{~m} / \mathrm{s}\right)$ and ambient temperature.

The pressure transducer used is an Endevco model 8507-C2 which is a circular deflectiontype transducer and has a flat frequency response from 0 to 70 kHz . The transducer was mounted inside the model and fixed to one of the windows. The transducer signal was amplified by a Measurements Group model 2310 strain gage conditioning amplifier.

Access to the flow field was provided through a 0.5 mm diameter pinhole. This pinhole and the associated dead volume have a second order frequency transfer function with a resonant frequency near 12 kHz as shown from calibrations ${ }^{7}$. Contributions of sources that are smaller than the pinhole area are spatially integrated, and thereby attenuated. This effect has been investigated, and $\operatorname{Corcos}^{8}$ provides a correction to the wall pressure spectrum in terms of $\omega d / 2 U_{C}$ where $\omega / U_{C}$ is the wave number. The correction given by Corcos ${ }^{8}$ was applied to the spectra presented here.

The pressure fluctuations were sampled at 71 kHz with 12 -bit precision. This sampling rate is higher than is commonly used. Twenty-five records of 16,384 data points each were
acquired at each location. During post-processing, each of these contiguous records was divided into sub-records and the time-delay subtraction was carried out. Spectral values were calculated using at least 500 averages. Additional bin averaging was performed to produce the final spectrum ${ }^{9}$. The spectra presented here are single-sided.

## References

1) Chesnakas, C. J., and Simpson, R. L., "Measurements of the Turbulence Structure in the Vicinity of a 3-D Separation," Journal of Fluids Engineering, Vol. 118, No. 1, 1996, pp. 268-275.
2) Ahn, S., and Simpson, R. L., "Cross-flow Separation on a Prolate Spheroid at Angles of Attack," AIAA Paper 92-0428, Jan. 1992.
3) Barber, K. M., and Simpson, R. L., "Mean Velocity and Turbulence Measurements of Flow Around a 6:1 Prolate Spheroid," AIAA Paper 91-0255, Jan. 1991.
4) Chesnakas, C. J., Simpson, R. L., and Madden, M. M., "Three Dimensional Velocity Measurements on a 6:1 Prolate Spheroid at Angle of Attack," Data Report VPI-AOE-202, Dept. of Aero \& Ocean Engr, VPI\&SU, Blacksburg, VA, Aug. 1993.
5) Chesnakas, C. J., and Simpson, R. L., "Full Three-Dimensional Measurements of the Cross-flow Separation Region of a 6:1 Prolate Spheroid," Experiments in Fluids, Vol. 17, 1994 pp. 68-74.
6) Chesnakas, C. J., and Simpson, R. L., "A Detailed Investigation of the 3-D Separation about a 6:1 Prolate Spheroid at Angle of Attack," AIAA Journal, Vol., 35, No. 6, 1997, pp. 990-999.
7) Goody, M.C., "An Experimental Investigation of Pressure Fluctuations in Three-Dimensional Turbulent Boundary Layers," Ph.D. Dissertation, Dept. of Aero \& Ocean Engr, VPI\&SU, Blacksburg, VA, 1999.
8) Corcos, G. M., "Resolution of Pressure in Turbulence," Journal of the Acoustical Society of America, Vol. 35, No. 2, 1963, pp. 192-199.
9) Bendat, J. S., and Piersol, A. G., Random Data: Analysis and Measurement, 2nd ed., Wiley, New York, 1986, pp. 252-290.
10) Goody, M. C., Simpson, R. L., Engel M., Chesnakas, C. J., and Devenport, W. J., "Mean Velocity and Pressure and Velocity Spectral Measurements within a Separated Flow Around a Prolate Spheroid at Incidence", AIAA Paper 98-0630, Jan. 1998.

Table 1. Some boundary layer parameters of the flow at $\alpha=10^{\circ}, x / L=0.600$.

| $\phi$ <br> deg | $\rho$ <br> $\mathrm{kg} / \mathrm{m}^{3}$ | $v\left(\times 10^{5}\right)$ <br> $\mathrm{m}^{2} / \mathrm{s}$ | $u_{\tau}^{\dagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{e}{ }^{\ddagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{\infty}$ <br> $\mathrm{m} / \mathrm{s}$ | $\delta^{* \ddagger}$ <br> mm | $d^{+\dagger}$ | $R e_{\theta}{ }^{\ddagger}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 1.05 | 1.79 | 2.45 | 54.8 | 54.7 | 1.16 | 68 | 2483 |
| 95 | 1.05 | 1.80 | 2.42 | 55.3 | 55.2 | 1.25 | 67 | 2673 |
| 100 | 1.05 | 1.80 | 2.36 | 55.3 | 55.2 | 1.35 | 65 | 2863 |
| 105 | 1.05 | 1.80 | 2.31 | 55.3 | 55.2 | 1.45 | 64 | 3073 |
| 110 | 1.06 | 1.78 | 2.23 | 54.8 | 54.6 | 1.56 | 62 | 3283 |
| 115 | 1.06 | 1.78 | 2.17 | 54.7 | 54.4 | 1.79 | 61 | 3739 |
| 120 | 1.06 | 1.76 | 2.10 | 54.2 | 53.9 | 2.01 | 60 | 4195 |
| 125 | 1.10 | 1.67 | 1.91 | 51.3 | 51.1 | 2.34 | 57 | 4797 |
| 130 | 1.10 | 1.66 | 1.82 | 51.1 | 50.9 | 2.66 | 55 | 5399 |
| 135 | 1.10 | 1.66 | 1.76 | 50.9 | 50.7 | 3.03 | 53 | 6084 |
| 140 | 1.10 | 1.66 | 1.70 | 50.9 | 50.7 | 3.40 | 51 | 6770 |
| 145 | 1.10 | 1.66 | 1.70 | 50.9 | 50.7 | 3.58 | 51 | 7182 |
| 150 | 1.10 | 1.65 | 1.70 | 50.8 | 50.6 | 3.76 | 51 | 7594 |
| 155 | 1.10 | 1.66 | 1.74 | 51.0 | 50.8 | 3.65 | 52 | 7501 |
| 160 | 1.10 | 1.66 | 1.77 | 51.0 | 50.8 | 3.55 | 53 | 7407 |
| 165 | 1.10 | 1.66 | 1.82 | 51.2 | 50.8 | 3.30 | 55 | 7031 |
| 170 | 1.10 | 1.66 | 1.88 | 51.6 | 51.0 | 3.05 | 56 | 6654 |
| 175 | 1.10 | 1.66 | 1.90 | 51.6 | 51.0 | 2.86 | 57 | 6254 |
| 180 | 1.10 | 1.66 | 1.92 | 51.5 | 51.0 | 2.67 | 58 | 5855 |

${ }^{\dagger}$ Calculated using the $C_{f}$ measurements of Chesnakas and Simpson ${ }^{6}$
${ }^{\ddagger}$ Calculated using the $\delta^{*}, \theta$, and $U_{e} / U_{\infty}$ measurements of Goody et al. ${ }^{10}$

Table 2. Some boundary layer parameters of the flow at $\alpha=10^{\circ}, x / L=0.772$.

| $\phi$ <br> deg | $\rho$ <br> $\mathrm{kg} / \mathrm{m}^{3}$ | $v\left(\times 10^{5}\right)$ <br> $\mathrm{m}^{2} / \mathrm{s}$ | $u_{\tau}{ }^{\dagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{e}{ }^{\ddagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{\infty}$ <br> $\mathrm{m} / \mathrm{s}$ | $\delta^{* \ddagger}$ <br> mm | $d^{+\dagger}$ | $R e_{\theta}{ }^{\ddagger}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 1.06 | 1.79 | 2.25 | 58.0 | 54.7 | 1.47 | 63 | 3145 |
| 95 | 1.05 | 1.80 | 2.23 | 58.0 | 55.0 | 1.59 | 62 | 3368 |
| 100 | 1.05 | 1.79 | 2.19 | 57.3 | 54.8 | 1.70 | 61 | 3592 |
| 105 | 1.06 | 1.79 | 2.07 | 56.8 | 54.7 | 1.99 | 58 | 4122 |
| 110 | 1.06 | 1.77 | 1.94 | 55.9 | 54.1 | 2.28 | 55 | 4651 |
| 115 | 1.07 | 1.76 | 1.82 | 55.3 | 53.8 | 2.79 | 52 | 5555 |
| 120 | 1.07 | 1.75 | 1.70 | 54.9 | 53.6 | 3.31 | 49 | 6458 |
| 125 | 1.07 | 1.74 | 1.65 | 54.6 | 53.4 | 4.06 | 47 | 7716 |
| 130 | 1.07 | 1.74 | 1.50 | 56.2 | 53.2 | 5.62 | 43 | 10417 |
| 135 | 1.07 | 1.73 | 1.47 | 55.6 | 53.1 | 6.39 | 42 | 11636 |
| 140 | 1.07 | 1.74 | 1.50 | 55.2 | 53.2 | 7.33 | 43 | 13394 |
| 145 | 1.07 | 1.74 | 1.61 | 54.4 | 53.2 | 7.24 | 46 | 14016 |
| 150 | 1.07 | 1.73 | 1.71 | 53.5 | 53.1 | 7.16 | 49 | 14637 |
| 155 | 1.08 | 1.73 | 1.84 | 52.5 | 52.9 | 5.81 | 53 | 12549 |
| 160 | 1.08 | 1.72 | 1.95 | 51.3 | 52.6 | 4.47 | 57 | 10640 |
| 165 | 1.09 | 1.70 | 2.01 | 51.2 | 52.0 | 3.57 | 59 | 8430 |
| 170 | 1.09 | 1.69 | 2.08 | 51.4 | 51.7 | 2.67 | 62 | 6400 |
| 175 | 1.09 | 1.68 | 2.06 | 51.3 | 51.5 | 2.25 | 61 | 5307 |
| 180 | 1.10 | 1.67 | 2.02 | 50.9 | 51.0 | 1.83 | 61 | 4213 |

${ }^{\dagger}$ Calculated using the $C_{f}$ measurements of Chesnakas and Simpson ${ }^{6}$
${ }^{*}$ Calculated using the $\delta^{*}, \theta$, and $U_{e} / U_{\infty}$ measurements of Goody et al. ${ }^{10}$

Table 3. Some boundary layer parameters of the flow at $\alpha=20^{\circ}, x / L=0.600$.

| $\phi$ <br> deg | $\rho$ <br> $\mathrm{kg} / \mathrm{m}^{3}$ | $v\left(\times 10^{5}\right)$ <br> $\mathrm{m}^{2} / \mathrm{s}$ | $u_{\tau}{ }^{\dagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{e}{ }^{\ddagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{\infty}$ <br> $\mathrm{m} / \mathrm{s}$ | $\delta^{* \ddagger}$ <br> mm | $d^{+\dagger}$ | $R e_{\theta}{ }^{\ddagger}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 1.10 | 1.66 | 2.55 | 51.0 | 50.9 | 0.67 | 77 | 1406 |
| 95 | 1.10 | 1.66 | 2.47 | 51.0 | 50.9 | 0.76 | 74 | 1586 |
| 100 | 1.10 | 1.66 | 2.38 | 50.9 | 50.9 | 0.85 | 71 | 1767 |
| 105 | 1.10 | 1.66 | 2.24 | 50.9 | 50.9 | 1.01 | 67 | 2056 |
| 110 | 1.10 | 1.66 | 2.10 | 50.9 | 50.9 | 1.18 | 63 | 2346 |
| 115 | 1.10 | 1.66 | 1.88 | 50.8 | 50.9 | 1.80 | 56 | 3358 |
| 120 | 1.10 | 1.66 | 1.62 | 50.8 | 50.9 | 2.42 | 49 | 4370 |
| 125 | 1.10 | 1.66 | 1.41 | 50.6 | 50.9 | 3.5 | 43 | 5790 |
| 130 | 1.10 | 1.66 | 1.29 | 50.4 | 50.9 | 4.98 | 39 | 10827 |
| 135 | 1.10 | 1.66 | 1.70 | 50.2 | 50.9 | 5.94 | 51 | 10546 |
| 140 | 1.10 | 1.66 | 1.91 | 50.0 | 50.9 | 6.24 | 57 | 12940 |
| 145 | 1.10 | 1.66 | 1.88 | 56.1 | 50.9 | 5.47 | 57 | 12242 |
| 150 | 1.10 | 1.66 | 2.44 | 54.8 | 50.9 | 4.57 | 73 | 10889 |
| 155 | 1.10 | 1.66 | 2.88 | 51.8 | 50.9 | 4.34 | 87 | 10405 |
| 160 | 1.10 | 1.66 | 3.04 | 49.5 | 50.9 | 4.00 | 92 | 9493 |
| 165 | 1.10 | 1.66 | 2.93 | 49.9 | 50.9 | 2.14 | 88 | 5045 |
| 170 | 1.10 | 1.66 | 2.80 | 50.4 | 50.9 | 0.28 | 84 | 597 |
| 175 | 1.10 | 1.66 | 2.71 | 50.7 | 50.9 | 0.37 | 81 | 781 |
| 180 | 1.10 | 1.66 | 2.61 | 51.0 | 50.9 | 0.45 | 78 | 965 |

${ }^{\dagger}$ Calculated using the $C_{f}$ measurements of Chesnakas and Simpson ${ }^{6}$
${ }^{*}$ Calculated using the $\delta^{*}, \theta$, and $U_{e} / U_{\infty}$ measurements of Goody et al. ${ }^{10}$

Table 4. Some boundary layer parameters of the flow at $\alpha=20^{\circ}, x / L=0.772$.

| $\phi$ <br> deg | $\rho$ <br> $\mathrm{kg} / \mathrm{m}^{3}$ | $v\left(\times 10^{5}\right)$ <br> $\mathrm{m}^{2} / \mathrm{s}$ | $u_{\tau}{ }^{\dagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{e}{ }^{\ddagger}$ <br> $\mathrm{m} / \mathrm{s}$ | $U_{\infty}$ <br> $\mathrm{m} / \mathrm{s}$ | $\delta^{* \ddagger}$ <br> mm | $d^{+\dagger}$ | $R e_{\theta}{ }^{\ddagger}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 90 | 1.07 | 1.74 | 2.36 | 59.4 | 53.3 | 0.82 | 68 | 1647 |
| 95 | 1.06 | 1.77 | 2.21 | 64.7 | 54.3 | 1.05 | 62 | 2055 |
| 100 | 1.06 | 1.77 | 2.00 | 68.8 | 54.3 | 1.28 | 56 | 2462 |
| 105 | 1.06 | 1.77 | 1.82 | 57.6 | 54.2 | 1.75 | 51 | 3249 |
| 110 | 1.05 | 1.79 | 1.56 | 57.5 | 54.9 | 2.60 | 44 | 4458 |
| 115 | 1.05 | 1.79 | 1.35 | 56.8 | 54.9 | 3.80 | 38 | 5910 |
| 120 | 1.06 | 1.78 | 1.53 | 55.7 | 54.5 | 5.19 | 43 | 8136 |
| 125 | 1.05 | 1.80 | 1.96 | 57.1 | 55.3 | 6.23 | 54 | 11434 |
| 130 | 1.05 | 1.80 | 2.29 | 57.7 | 55.1 | 7.28 | 64 | 14732 |
| 135 | 1.05 | 1.79 | 2.45 | 53.7 | 54.9 | 6.08 | 68 | 13550 |
| 140 | 1.05 | 1.80 | 2.62 | 50.2 | 55.3 | 4.88 | 73 | 12368 |
| 145 | 1.05 | 1.80 | 1.83 | 56.4 | 55.3 | 6.40 | 51 | 14625 |
| 150 | 1.05 | 1.80 | 2.21 | 57.3 | 55.1 | 5.29 | 61 | 13406 |
| 155 | 1.05 | 1.80 | 3.08 | 56.2 | 55.3 | 3.52 | 85 | 8935 |
| 160 | 1.05 | 1.79 | 3.29 | 55.5 | 54.9 | 2.60 | 92 | 6348 |
| 165 | 1.06 | 1.78 | 3.20 | 56.8 | 54.5 | 1.44 | 90 | 3474 |
| 170 | 1.05 | 1.80 | 3.15 | 58.9 | 55.0 | 0.28 | 88 | 600 |
| 175 | 1.05 | 1.79 | 2.99 | 58.0 | 54.8 | 0.34 | 84 | 727 |
| 180 | 1.05 | 1.79 | 2.83 | 57.2 | 54.8 | 0.39 | 79 | 854 |

${ }^{\dagger}$ Calculated using the $C_{f}$ measurements of Chesnakas and Simpson ${ }^{6}$
${ }^{*}$ Calculated using the $\delta^{*}, \theta$, and $U_{e} / U_{\infty}$ measurements of Goody et al. ${ }^{10}$

Table 5. Variation of $\overline{p^{2}} / Q_{\infty}^{2}$ with $\phi$ at $\alpha=10^{\circ}, x / L=0.600$ showing the contribution of various frequency ranges to the $\overline{p^{2}}$ integral including the Analytical Integral Contribution (AIC). The values presented here were calculated by integrating the $p$ spectra.

| $\phi$ | Total $\overline{p^{2}} / Q_{\infty}^{2}$ | Contribution to $\overline{p^{2}} / Q_{\infty}^{2}$ |  |  |  |  | $\left(\times 10^{5}\right)$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| deg | $\left(\times 10^{5}\right)$ | $f \leq 994 \mathrm{~Hz}$ | $994 \mathrm{~Hz}<f \leq 25 \mathrm{kHz}$ | $f>25 \mathrm{kHz}$ (AIC) |  |  |  |  |  |
| 90 | 14.5 | 2.5 | $17 \%$ | 8.7 | $60 \%$ | 3.3 | $23 \%$ |  |  |
| 95 | 13.2 | 2.4 | $18 \%$ | 8.1 | $61 \%$ | 2.7 | $21 \%$ |  |  |
| 100 | 12.2 | 2.3 | $19 \%$ | 7.8 | $64 \%$ | 2.1 | $17 \%$ |  |  |
| 105 | 11.1 | 2.2 | $20 \%$ | 7.2 | $65 \%$ | 1.7 | $15 \%$ |  |  |
| 110 | 10.4 | 2.3 | $22 \%$ | 6.9 | $66 \%$ | 1.2 | $12 \%$ |  |  |
| 115 | 9.6 | 2.3 | $24 \%$ | 6.4 | $67 \%$ | 0.9 | $9 \%$ |  |  |
| 120 | 9.3 | 2.5 | $28 \%$ | 6.1 | $65 \%$ | 0.7 | $7 \%$ |  |  |
| 125 | 7.9 | 2.1 | $26 \%$ | 5.5 | $70 \%$ | 0.3 | $4 \%$ |  |  |
| 130 | 7.1 | 2.1 | $29 \%$ | 4.8 | $68 \%$ | 0.2 | $3 \%$ |  |  |
| 135 | 6.4 | 2.1 | $32 \%$ | 4.2 | $66 \%$ | 0.1 | $2 \%$ |  |  |
| 140 | 6.1 | 2.2 | $36 \%$ | 3.8 | $63 \%$ | 0.09 | $1 \%$ |  |  |
| 145 | 5.4 | 1.9 | $35 \%$ | 3.4 | $63 \%$ | 0.09 | $2 \%$ |  |  |
| 150 | 5.5 | 2.0 | $36 \%$ | 3.4 | $63 \%$ | 0.09 | $1 \%$ |  |  |
| 155 | 5.7 | 2.0 | $34 \%$ | 3.6 | $64 \%$ | 0.1 | $2 \%$ |  |  |
| 160 | 6.1 | 2.0 | $33 \%$ | 4.0 | $65 \%$ | 0.1 | $2 \%$ |  |  |
| 165 | 6.8 | 2.0 | $30 \%$ | 4.6 | $67 \%$ | 0.2 | $3 \%$ |  |  |
| 170 | 7.5 | 2.0 | $27 \%$ | 5.2 | $69 \%$ | 0.3 | $4 \%$ |  |  |
| 175 | 7.9 | 2.1 | $26 \%$ | 5.5 | $70 \%$ | 0.3 | $4 \%$ |  |  |
| 180 | 8.0 | 2.0 | $25 \%$ | 5.6 | $70 \%$ | 0.4 | $5 \%$ |  |  |

Table 6. Variation of $\overline{p^{2}} / Q_{\infty}^{2}$ with $\phi$ at $\alpha=10^{\circ}, x / L=0.772$ showing the contribution of various frequency ranges to the $\overline{p^{2}}$ integral including the Analytical Integral Contribution (AIC). The values presented here were calculated by integrating the $p$ spectra.

| $\phi$ | Total $\overline{p^{2}} / Q_{\infty}^{2}$ | Contribution to $\overline{p^{2}} / Q_{\infty}^{2}$ |  |  |  |  | $\left(\times 10^{5}\right)$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| deg | $\left(\times 10^{5}\right)$ | $f \leq 994 \mathrm{~Hz}$ | $994 \mathrm{~Hz}<f \leq 25 \mathrm{kHz}$ | $f>25 \mathrm{kHz}$ (AIC) |  |  |  |  |  |
| 90 | 11.9 | 2.3 | $19 \%$ | 8.2 | $69 \%$ | 1.4 | $12 \%$ |  |  |
| 95 | 11.0 | 2.3 | $21 \%$ | 7.6 | $68 \%$ | 1.2 | $11 \%$ |  |  |
| 100 | 10.4 | 2.4 | $24 \%$ | 7.0 | $67 \%$ | 1.0 | $9 \%$ |  |  |
| 105 | 9.3 | 2.4 | $25 \%$ | 6.4 | $69 \%$ | 0.5 | $6 \%$ |  |  |
| 110 | 8.9 | 3.0 | $34 \%$ | 5.6 | $63 \%$ | 0.3 | $3 \%$ |  |  |
| 115 | 7.9 | 3.0 | $37 \%$ | 4.8 | $61 \%$ | 0.1 | $2 \%$ |  |  |
| 120 | 6.6 | 2.7 | $41 \%$ | 3.8 | $58 \%$ | 0.06 | $1 \%$ |  |  |
| 125 | 5.8 | 2.8 | $47 \%$ | 3.0 | $52 \%$ | 0.04 | $1 \%$ |  |  |
| 130 | 5.0 | 2.6 | $53 \%$ | 2.4 | $47 \%$ | 0.01 | $0 \%$ |  |  |
| 135 | 4.5 | 2.7 | $60 \%$ | 1.8 | $40 \%$ | 0.01 | $0 \%$ |  |  |
| 140 | 4.1 | 2.5 | $60 \%$ | 1.6 | $40 \%$ | 0.01 | $0 \%$ |  |  |
| 145 | 4.5 | 2.3 | $51 \%$ | 2.2 | $48 \%$ | 0.03 | $1 \%$ |  |  |
| 150 | 5.6 | 2.4 | $43 \%$ | 3.1 | $56 \%$ | 0.07 | $1 \%$ |  |  |
| 155 | 6.7 | 2.3 | $35 \%$ | 4.2 | $63 \%$ | 0.2 | $2 \%$ |  |  |
| 160 | 8.1 | 2.2 | $27 \%$ | 5.6 | $69 \%$ | 0.3 | $4 \%$ |  |  |
| 165 | 9.6 | 2.3 | $24 \%$ | 6.8 | $71 \%$ | 0.5 | $5 \%$ |  |  |
| 170 | 10.3 | 2.0 | $19 \%$ | 7.5 | $73 \%$ | 0.8 | $8 \%$ |  |  |
| 175 | 10.5 | 2.0 | $20 \%$ | 7.7 | $73 \%$ | 0.8 | $7 \%$ |  |  |
| 180 | 10.7 | 2.2 | $21 \%$ | 7.8 | $73 \%$ | 0.7 | $6 \%$ |  |  |
|  |  |  |  |  |  |  |  |  |  |

Table 7. Variation of $\overline{p^{2}} / Q_{\infty}^{2}$ with $\phi$ at $\alpha=20^{\circ}, x / L=0.600$ showing the contribution of various frequency ranges to the $\overline{p^{2}}$ integral including the Analytical Integral Contribution (AIC). The values presented here were calculated by integrating the $p$ spectra.

| $\phi$ | Total $\overline{p^{2}} / Q_{\infty}^{2}$ | Contribution to $\overline{p^{2}} / Q_{\infty}^{2}$ |  |  |  |  | $\left(\times 10^{5}\right)$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| deg | $\left(\times 10^{5}\right)$ | $f \leq 994 \mathrm{~Hz}$ | $994 \mathrm{~Hz}<f \leq 25 \mathrm{kHz}$ | $f>25 \mathrm{kHz}$ (AIC) |  |  |  |  |  |
| 90 | 26.8 | 1.9 | $7 \%$ | 11.4 | $43 \%$ | 13.5 | $50 \%$ |  |  |
| 95 | 24.4 | 1.9 | $8 \%$ | 11.4 | $46 \%$ | 11.1 | $46 \%$ |  |  |
| 100 | 21.3 | 2.0 | $9 \%$ | 11.1 | $52 \%$ | 8.2 | $39 \%$ |  |  |
| 105 | 17.9 | 2.0 | $11 \%$ | 10.5 | $59 \%$ | 5.4 | $30 \%$ |  |  |
| 110 | 14.7 | 2.2 | $15 \%$ | 9.7 | $66 \%$ | 2.8 | $19 \%$ |  |  |
| 115 | 11.5 | 2.4 | $20 \%$ | 8.4 | $73 \%$ | 0.7 | $7 \%$ |  |  |
| 120 | 10.1 | 2.8 | $28 \%$ | 7.1 | $70 \%$ | 0.2 | $2 \%$ |  |  |
| 125 | 8.2 | 3.3 | $41 \%$ | 4.9 | $59 \%$ | 0.03 | $0 \%$ |  |  |
| 130 | 6.1 | 3.5 | $58 \%$ | 2.6 | $42 \%$ | 0.01 | $0 \%$ |  |  |
| 135 | 5.5 | 3.1 | $57 \%$ | 2.3 | $42 \%$ | 0.07 | $1 \%$ |  |  |
| 140 | 9.2 | 4.1 | $44 \%$ | 4.7 | $51 \%$ | 0.4 | $5 \%$ |  |  |
| 145 | 12.3 | 3.9 | $32 \%$ | 7.3 | $59 \%$ | 1.1 | $9 \%$ |  |  |
| 150 | 24.9 | 4.0 | $16 \%$ | 9.9 | $40 \%$ | 11.0 | $44 \%$ |  |  |
| 155 | 45.2 | 4.2 | $9 \%$ | 10.9 | $24 \%$ | 30.1 | $67 \%$ |  |  |
| 160 | 58.3 | 4.0 | $7 \%$ | 11.8 | $20 \%$ | 42.5 | $73 \%$ |  |  |
| 165 | 46.8 | 3.2 | $7 \%$ | 11.9 | $25 \%$ | 31.7 | $68 \%$ |  |  |
| 170 | 38.0 | 2.7 | $7 \%$ | 12.0 | $32 \%$ | 23.3 | $61 \%$ |  |  |
| 175 | 30.5 | 2.0 | $7 \%$ | 11.1 | $36 \%$ | 17.4 | $57 \%$ |  |  |
| 180 | 27.1 | 2.1 | $8 \%$ | 10.8 | $40 \%$ | 14.2 | $52 \%$ |  |  |

Table 8. Variation of $\overline{p^{2}} / Q_{\infty}^{2}$ with $\phi$ at $\alpha=20^{\circ}, x / L=0.772$ showing the contribution of various frequency ranges to the $\overline{p^{2}}$ integral including the Analytical Integral Contribution (AIC). The values presented here were calculated by integrating the $p$ spectra.

| $\phi$ | Total $\overline{p^{2}} / Q_{\infty}^{2}$ | Contribution to $\overline{p^{2}} / Q_{\infty}^{2}$ |  |  |  |  | $\left(\times 10^{5}\right)$ |  |
| :---: | :---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: |
| deg | $\left(\times 10^{5}\right)$ | $f \leq 994 \mathrm{~Hz}$ | $994 \mathrm{~Hz}<f \leq 23 \mathrm{kHz}$ | $f>23 \mathrm{kHz}$ (AIC) |  |  |  |  |
| 90 | 22.4 | 3.1 | $14 \%$ | 11.2 | $50 \%$ | 8.1 | $36 \%$ |  |
| 95 | 18.7 | 3.3 | $18 \%$ | 10.8 | $58 \%$ | 4.6 | $24 \%$ |  |
| 100 | 15.6 | 3.8 | $24 \%$ | 10.0 | $65 \%$ | 1.8 | $11 \%$ |  |
| 105 | 12.9 | 4.1 | $32 \%$ | 8.3 | $64 \%$ | 0.5 | $4 \%$ |  |
| 110 | 10.5 | 4.5 | $43 \%$ | 5.9 | $56 \%$ | 0.07 | $1 \%$ |  |
| 115 | 8.2 | 5.4 | $66 \%$ | 2.8 | $34 \%$ | 0.006 | $0 \%$ |  |
| 120 | 9.9 | 6.1 | $62 \%$ | 3.7 | $37 \%$ | 0.08 | $1 \%$ |  |
| 125 | 14.9 | 6.6 | $45 \%$ | 7.2 | $48 \%$ | 1.1 | $7 \%$ |  |
| 130 | 27.4 | 9.6 | $35 \%$ | 13.7 | $50 \%$ | 4.1 | $15 \%$ |  |
| 135 | 44.9 | 22.0 | $49 \%$ | 17.2 | $38 \%$ | 5.7 | $13 \%$ |  |
| 140 | 18.2 | 9.0 | $50 \%$ | 6.8 | $37 \%$ | 2.4 | $13 \%$ |  |
| 145 | 23.9 | 10.0 | $42 \%$ | 13.3 | $55 \%$ | 0.6 | $3 \%$ |  |
| 150 | 35.8 | 18.3 | $51 \%$ | 11.7 | $33 \%$ | 5.8 | $16 \%$ |  |
| 155 | 59.5 | 8.0 | $14 \%$ | 10.2 | $17 \%$ | 41.3 | $69 \%$ |  |
| 160 | 66.8 | 4.4 | $7 \%$ | 11.0 | $16 \%$ | 51.4 | $77 \%$ |  |
| 165 | 54.9 | 2.7 | $5 \%$ | 11.0 | $20 \%$ | 41.2 | $75 \%$ |  |
| 170 | 47.5 | 2.6 | $6 \%$ | 10.5 | $22 \%$ | 34.4 | $72 \%$ |  |
| 175 | 40.2 | 2.3 | $6 \%$ | 10.6 | $26 \%$ | 27.3 | $68 \%$ |  |
| 180 | 34.7 | 2.4 | $7 \%$ | 10.1 | $29 \%$ | 22.2 | $64 \%$ |  |
|  |  |  |  |  |  |  |  |  |

